

A State of Art on Different Configurations of Permanent Magnet Brushless Machines

Bhim Singh, *Fellow*

B P Singh, *Fellow*

S Dwivedi, *Non-member*

The highest efficiency, fast dynamic response and high power density of permanent magnet brushless (PMBL) machines are resulting in their wide spread applications. There are various type of these machines including permanent magnet synchronous motors (PMSM), permanent magnet brushless dc motors (PMBLDM) and hybrid doubly salient motors. This paper presents a comprehensive review of different configurations of PMBL machines, their rotor geometries and application potential, state of art and recent trends in PMBL machines. A classified list of more than one hundred research publications on the subject is appended for quick reference.

Keywords : Permanent magnet; Axial flux; Radial flux; Rotor geometries; Classification of PMBL machines

INTRODUCTION

Permanent magnet brushless (PMBL) machines are achieving increasing popularity due to advancement in geometries and design innovations. PMBL machines are best suited for position control and medium size industrial drive due to their excellent dynamic capability, reduced losses and high torque/weight ratio¹⁻²⁸. These machines are becoming popular due to availability of cost effective rare earth PM materials like Sm-Co and Nd-Fe-B. Availability of these high energy density PM materials not only enhances the performance of PMBLM drive but also reduces the size and losses in these machines. The PM excitation has been used in place of dc excitation in different PMBL machines to get brushless construction with reduced maintenance cost and increased life²⁹⁻³⁹. The various configurations of PMBL machines include PMSM, PMBLDC motors, axial flux permanent magnet (AFPM) machines, PM alternators and torous alternators⁴⁰⁻⁸⁰. The different rotor geometries include surface type, interior type, radial and axial field machines. Permanent magnet machines have found wide range applications in various fields such as domestic equipments, automobiles, transportation, aerospace equipment, power tools, toys, vision and sound equipments and healthcare equipments ranging from microwatt to megawatts. With the advancement in power electronics and PM material technology it is possible to design PM generators for power generation board on ships, aircraft, hybrid electric cars and buses, with the saving in generator weight, size and their higher payload capacity for the complete vehicle. Recent developments in PM machines technology include availability of improved PM material, varying construction for motor and generators such as axial field, radial field, two phase, three phase, higher phases with different rotor geometries, hybrid configuration, rectangular fed motor, sinusoidal fed motor, improved sensor technology, fast semiconductor modules, low cost high performance microelectronics devices. New control approaches have been proven to use these machines suitable for position control in machine tools, robotics and high precision

Bhim Singh, B P Singh and S Dwivedi are with the Department of Electrical Engineering, IIT Delhi, Hauz Khas, New Delhi - 110 016

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servos, speed control and torque control in various industrial drives and process control applications. In spite of being most promising nature of these machines they have faced many hurdles to come to their present stage in terms of cost, torque ripple, noise, vibration, reduce reliability due to large number of components, operational constraints such as temperature rise *etc*⁸¹⁻¹¹³. Due to their unmatched advantages and wide range of applications of these PMBL machines, new finding in design, cost optimization and development are reported in new books and recent publications. Therefore, it is considered a timely attempt to present a broad perspective on the status of PMBL machines technology.

This paper deals with an exhaustive review of PMBL machines consisting an state of art on various PM materials, different types of constructions and various rotor configurations. The application potential¹¹⁴⁻¹²⁶ and futuristic trends are also presented in brief alongwith conclusive remarks.

DIFFERENT PERMANENT MAGNET MATERIALS

The properties of PM materials are having great influence on the performance of PMBL machines. These are used for excitation in machines for the application ranging from robotics to standard commercial drive to energy generating systems. PMAC machines have various advantages such as high efficiency and power factor, high torque to weight ratio, brushless construction etc.

It is equally important to know that which type of design and configuration is used in an electrical machine. The application requirement decides the type of PM material used due to cost, size and weight. It is very important to consider operating temperature range, external demagnetizing field, weight constraint and space limitation at design stage itself. PM motors of commercial characteristics use ceramic or polymer-bonded neodymium-iron-boron magnets. For high performance motors, where the size and weight constraints are present, there sintered rare earth magnets are used. In applications, where the motor is exposed to extreme environment, Alnico is preferred in these machines. The use of Nd-Fe-B based PM material makes it possible to design and develop an electrical machine of any size excited by fully or partially by these

Table 1 Different permanent magnetic materials

Name of Material	Type of Magnet	Br, T	Hc, kA/m	(BH)max KJ/m ³
Alnico-5	Alnico	1.28	50.90	43.76
Alnico-8	Alnico	0.92	127.30	47.76
Ceramic-5	Ceramic	0.38	183.00	27.85
Mn-Al-C	Ceramic	0.56	238.70	59.68
Co-17- R-2	Sm-Co rare earth	1.1	397.88	238.73
NdFeB, Vacodym (633HR)	Nd-Fe-B rare earth	1.3	1000.00	330.00

permanent magnets. Table 1 enlists a few available PM materials used in electrical rotating machines. Alnico magnets can carry flux densities equivalent to soft magnetic irons but they are easily demagnetized due to lower values of coercive force as compared to ceramic magnets. Ceramic magnets are cheap but limited by low maximum energy density product. It is due to lower values of retentivity. Rare earth PM materials such as samarium cobalt alloys have relatively more desirable magnetic properties, but these are expensive. Except the polymer bonded rare earth magnets, ferrites and cobalt based metallic magnets are physically hard and brittle. It is application specific to select the particular PM material but recent trends are to use Nd-Fe-B rare earth magnets due to its highest energy density and residual flux density amongst available PM materials²⁹⁻³⁹.

DIFFERENT CONFIGURATIONS OF PM BRUSHLESS MACHINES

PM machines can be classified into two broad categories of brushed and brushless construction. These PMBL machines can be further subdivided according to various criteria including mode of operation *ie*, motor or generator, direction of the magnetic field *ie*, axial or radial field machines, type of rotor, *ie*, different rotor geometries, rating of machines such as fractional kilowatts or high power machines, sensorless or with sensors. The PMBL motors can be further categorized as PM brushless dc Motors (PMBLDCM) and PM synchronous motors (PMSM). Among all of these configurations of PMBL motors, PMBLDCM and PMSM are most popular form of PMBL motors used in various applications. These different classifications of PMBL machines are shown in Figure 1 and various rotor geometries for radial field PM machines are given in Figures 2-24. Figures 25-28 show four schematics of axial field PM machines.

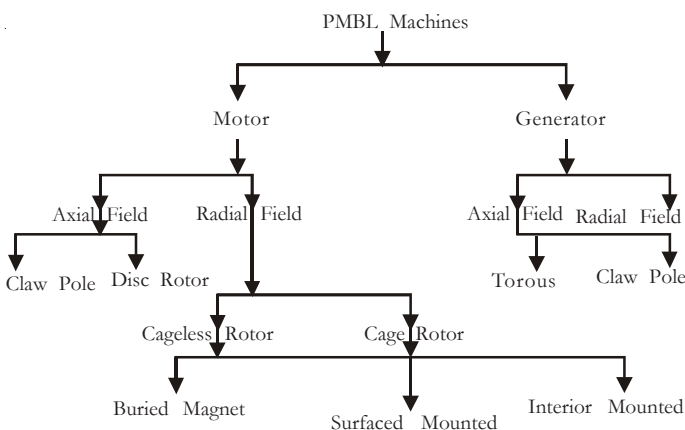


Figure 1 Classification of PM machines

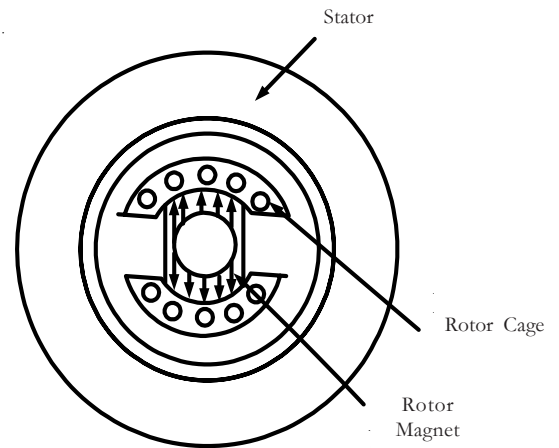


Figure 2 Classical configuration of embedded magnet rotor type PM machine

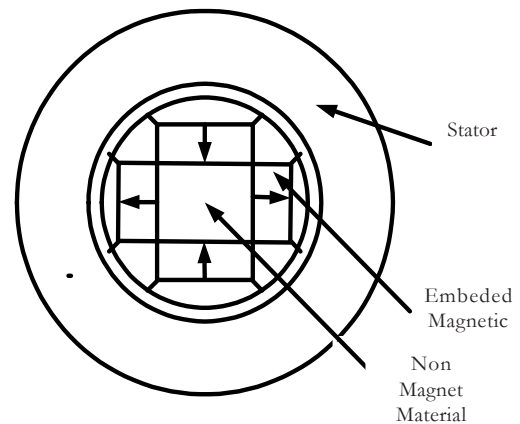


Figure 3 Buried magnet rotor type PM machine

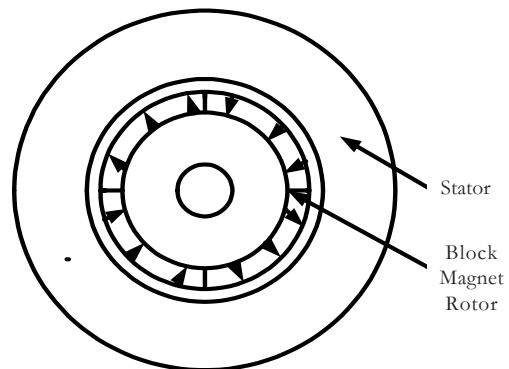


Figure 4 Bonded ring magnet rotor type PM machine

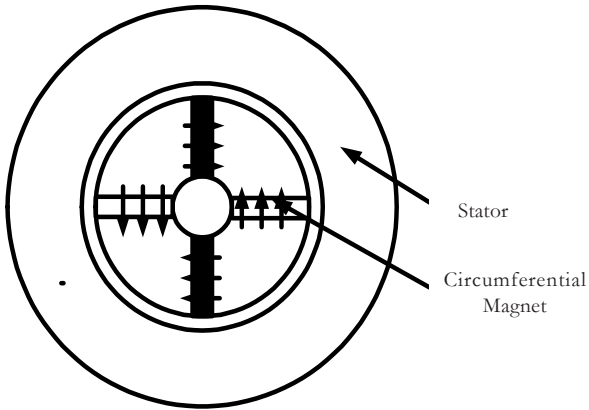


Figure 5 Circumferential magnet rotor type PM machine

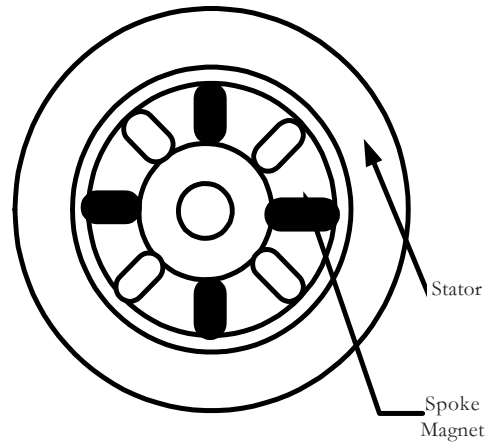


Figure 9 Spoke magnet rotor type PM machine

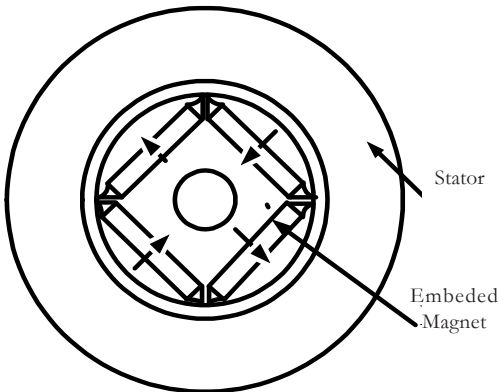


Figure 6 Embedded magnet rotor type PM machine

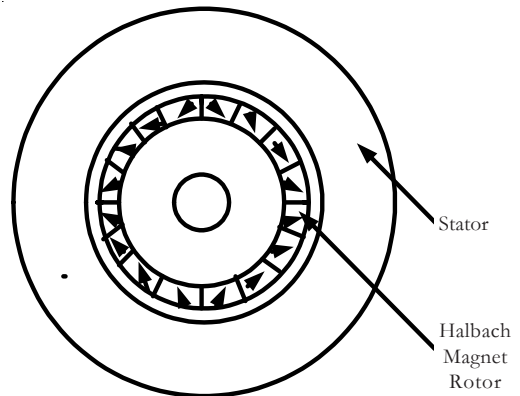


Figure 10 Halbach magnetized rotor type PM machine

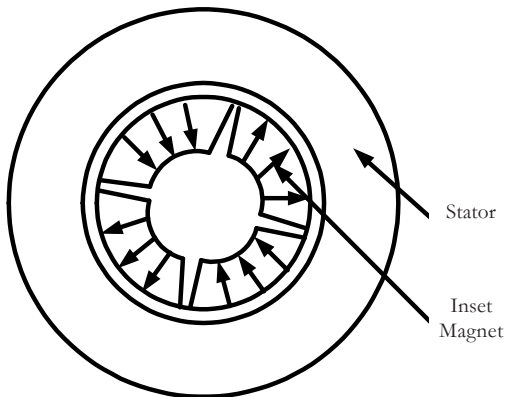


Figure 7 Inset magnet rotor type PM machine

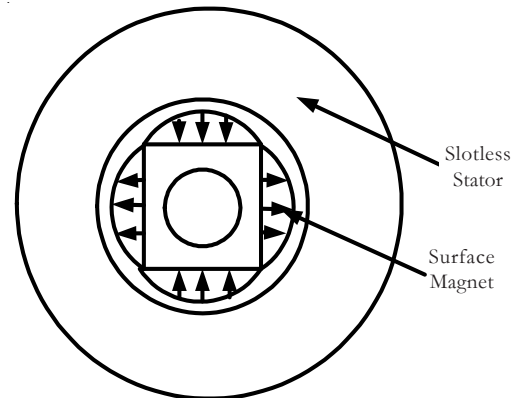


Figure 11 Slotless stator type PM machine

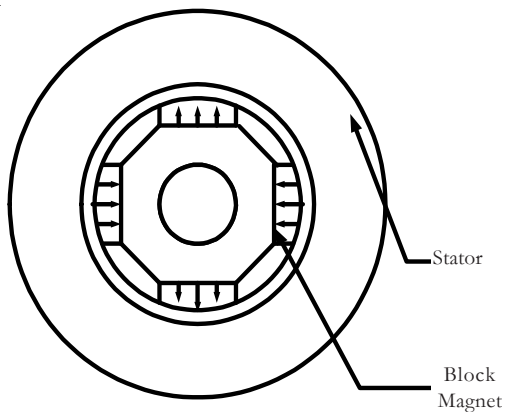


Figure 8 Block magnet rotor type PM machine

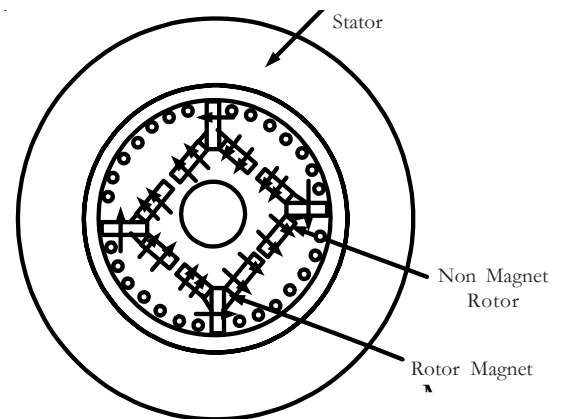


Figure 12 New design inset magnet rotor type PM machine

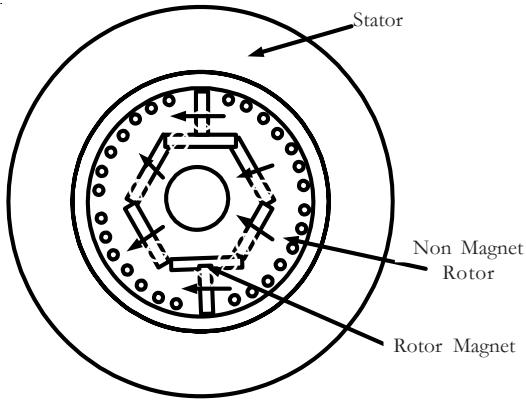


Figure 13 Specially direction magnetized rotor with cage type PM machine

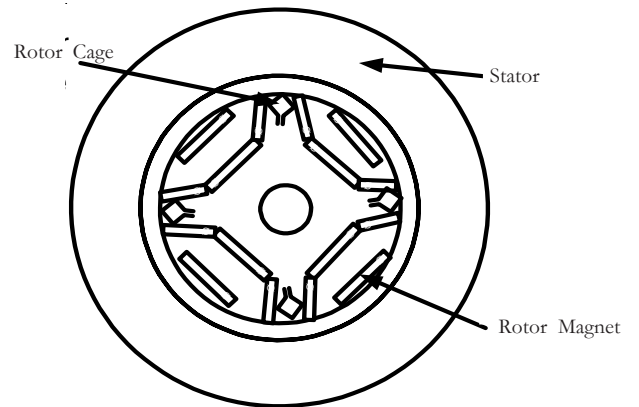


Figure 17 Interior double layer PM rotor type PM machine

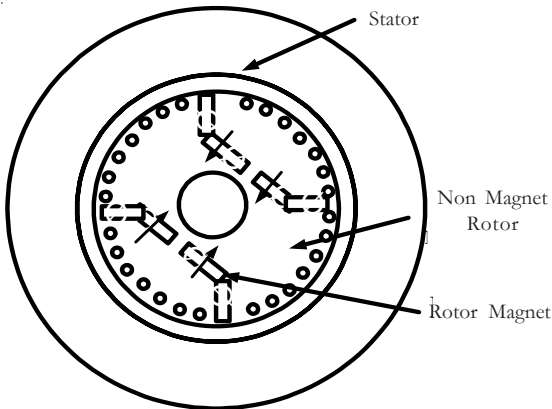


Figure 14 Inset magnet with damper bar rotor type PM machine

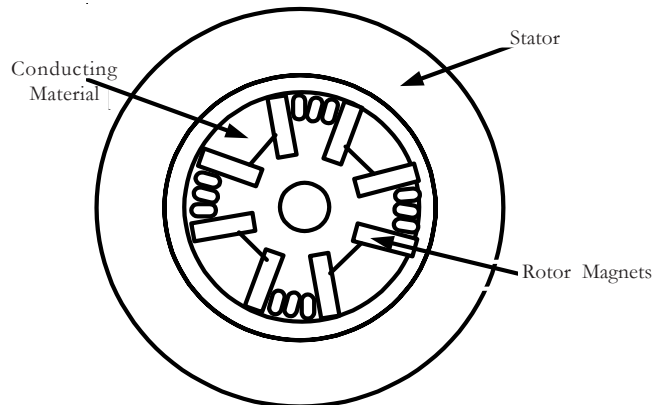


Figure 18 New design of PM rotor type PM machine

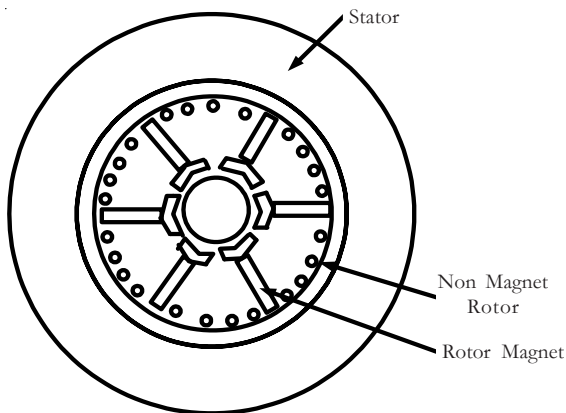


Figure 15 Radially magnetized rotor type PM machine

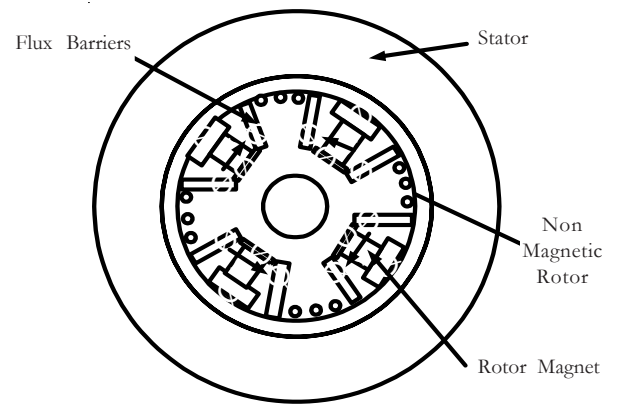


Figure 19 Hybrid magnetized rotor type PM machine

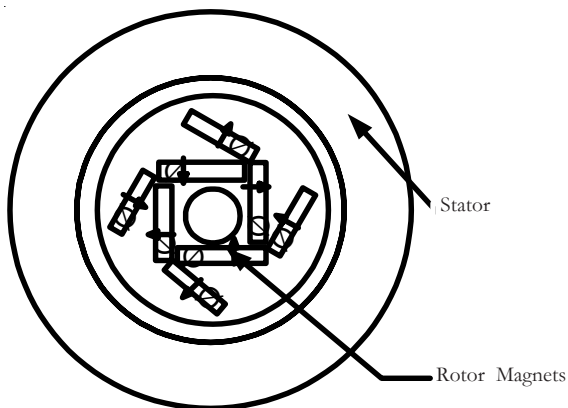


Figure 16 Special direction magnetized rotor type PM machine

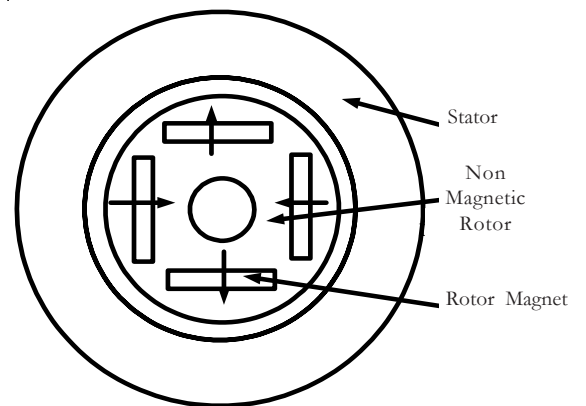


Figure 20 Classical configuration rotor type PM machine

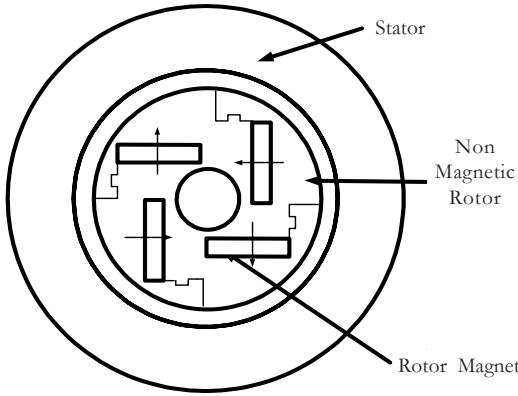


Figure 21 Rotor with buried magnets asymmetrically distributed rotor type PM machine

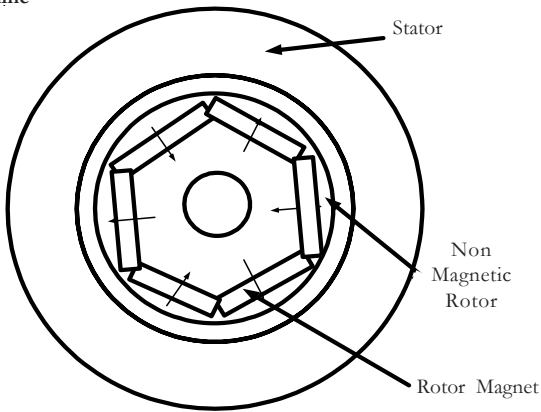


Figure 22 Interior six-pole magnet type rotor type PM machine

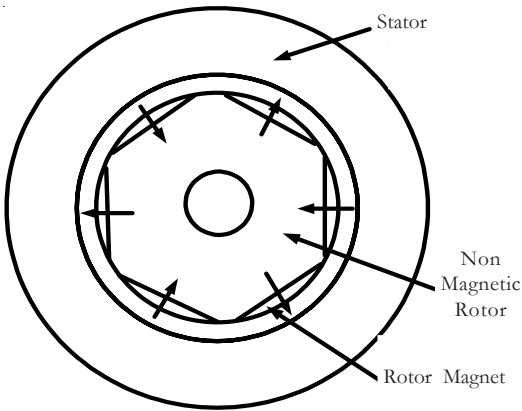


Figure 23 Bread loaf magnets rotor type PM machine

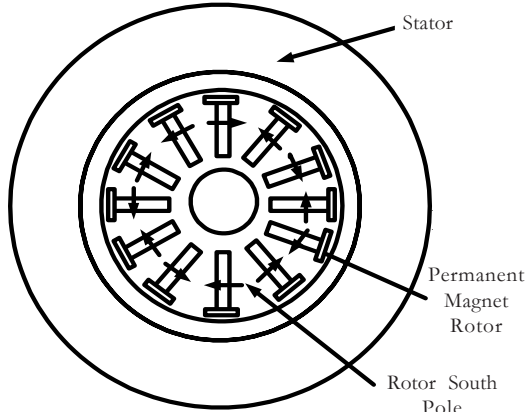


Figure 24 Tangentially magnetized rotor type PM machine

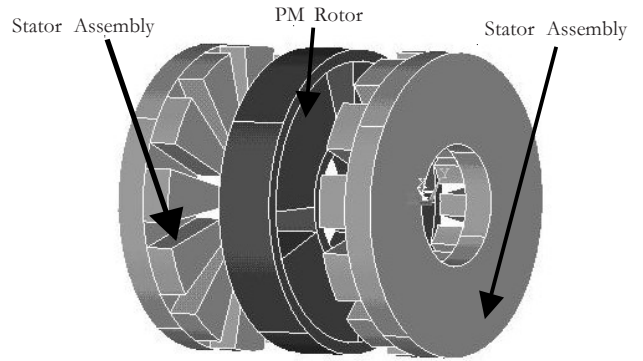


Figure 25 Axial field double stator PM synchronous motor

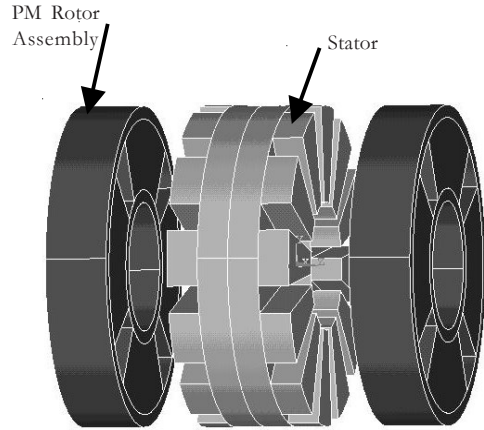


Figure 26 Axial field double rotor PM synchronous motor

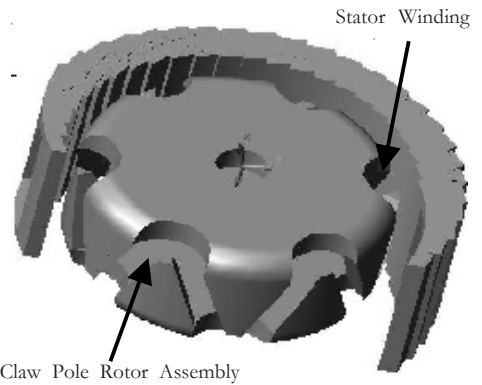


Figure 27 Claw pole rotor type PM axial flux alternator

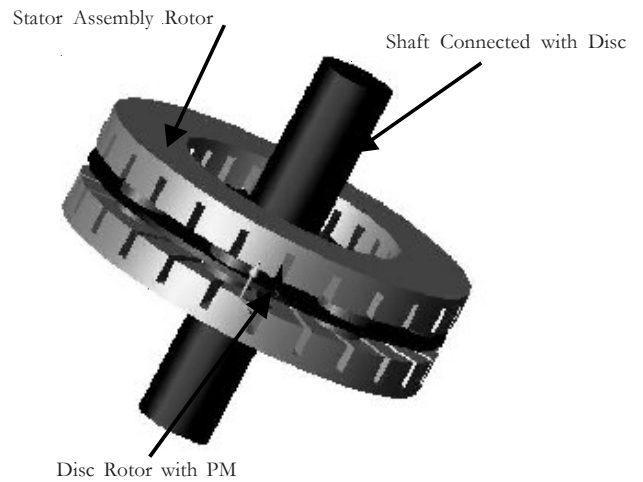


Figure 28 Disk rotor type PM axial flux alternator

The stator of PM synchronous motor is very similar to that of a polyphase induction motor. In last decade various geometries of PM synchronous motors have been used. They are usually based on the further improvements of power density and efficiency by adopting flux enhancement, armature reaction reduction and high-speed operation. Two main configurations of PM synchronous motors are surface magnet type where magnet are mounted on the outer surface of the rotor, and the buried magnet type where the magnets are mounted inside the magnetic structure of the rotor. Mounting the magnets to the surface of the rotor are the simplest and cheapest method for construction of PMBL motor. Surface mounted magnets are typically glued to the shaft and sometimes bonded with a non-conductive material. This surface mounting design tends to yield a small rotor diameter with small inertia, which is suitable for fast dynamic performance. Another type of surface magnet is the inset magnet motor. This machine has magnets that span less than one pole pitch mounted to the surface of the rotor, with an iron rotor tooth, filling the space between magnets. This design of a machine with a much higher reactance than one without the rotor tooth, has X_q larger than X_d . In this machine the saliency provides a significant reluctance torque as well as the magnet torque. The high reactance ratio makes it possible the flux weakening operation of PM synchronous motor and also helps to reduce harmonic copper losses in the motor. Another method for mounting the magnet on the surface of the rotor is to imbed them in the interior of the rotor. Interior design provides mechanical robustness and smaller air gap, which results in a component of reluctance torque in addition to the developed torque due to PM excitation.

Surface and interior magnet mounted designs are radially magnetized, therefore no-load flux density is limited to magnet flux density. If higher air gap flux density is required, the interior magnet design may be employed where the magnets are magnetized in the circumferential direction with the poles in opposition to concentrate the flux at the pole compared to magnet surface. The various type of PM rotor geometries include the permasyn motor⁴¹, siemosyn motor⁶, isosyn motor⁴¹, Binns PM rotor geometry configuration⁴¹ and GE design PM rotor⁶. Another type of PMBL machine is axial field machine in which direction of the magnetic field is axial instead of the radial field. The claw pole PM machines used in automobiles alternator and disk rotor machine with very low rotor inertia, are the example of axial flux machines. The various configurations of axial field PMBL machine include single stator and single rotor, single stator sandwiched between two rotors (double air gaps), single rotor sandwiched between two stators (double air gaps) and a variety of multiple stators and rotors (multiple air gaps)⁸⁸⁻¹⁰⁴. These different configurations of the PM machines are summarized in the Table 2. In this table different PM rotor geometries are compared on the basis of their advantages, limitations, power rating and field of applications.

APPLICATION POTENTIALS AND FUTURISTIC TRENDS

In the field of PMBL machines technology the current research

include search of high energy density PM materials, application of new rotor geometries for effective utilization of the magnet flux. The recent trends in PMBL machines are in the area of improvement in the design and manufacturing techniques, reduction and elimination of torque ripple and cogging torque by employing appropriate rotor geometry. The PM materials ranging from ferrite to alnico and rare earth magnets have gradually changed the cost and size of these PMBL machines¹⁻³⁹. Various types of PMBL machines include the PMSM and PMBLDC motor⁴⁰⁻⁸⁰. Application of finite element analysis (FEA) is used for the magnetic field computation and analysis of performance of PMBL machines with different rotor configurations. FEA is a useful tool for improving the existing design of PMBL machines towards the performance improvement and design optimization of these machines. The resulting PMBL machines are quite accurate and verifiable versus laboratory test data on these machines¹⁰⁵⁻¹¹³.

For high performance applications, torque smoothness is essential. It is very important to consider torque ripple minimization by design improvement or by using appropriate rotor geometry. The PMSM have great potential for both ripple torque and cogging torque minimization by adopting fractional slot pitch windings or skewing of the rotor magnet. Whereas PMBLDC motor requires controller based techniques for minimizing pulsating torque by means of active cancellation algorithm⁸¹⁻⁸⁷.

Axial flux permanent magnet (AFPM) machines are having ability to produce high torque. The PMBL machines have great potential for diverse applications ranging from high performance servo drive needed for precise tool manufacturing to energy efficient drive for various consumer product and industrial applications. Axial flux permanent magnet brushless motors develop high torque even in the low speed range with high power density and efficiency. The axial flux motor is used as a wheel to an electric motorbike and its characteristics are very promising for use in electric vehicles (EV's) applications¹¹⁸⁻¹²¹. In the aerospace applications PMBL generators are best suited due to its high specific output power (output power/volume), which helps in substantial fuel economy and improvements in payload capability of aircraft. Another application of PMBL machines are in ship where these machines are used for power generation and ship propulsion¹¹⁴⁻¹²⁶.

CONCLUSION

An exhaustive review of different configurations of PMBL machines has been presented, which includes use of new PM materials, different rotor geometries and their construction and optimization. The present status of permanent magnet machines has revealed that these machines have great potential for use in a number of applications. The latest manufacturing techniques, intelligent closed loop control, sensorless operation and field weakening have resulted in wide range applications and provided a broad prospective to these machines.

Table 2 Comparison of different PM rotor geometries

Sr No	Name of the Rotor Configuration	Advantages	Limitations	Power Rating	Application	Figure No
1.	Embedded magnet rotor	Line start, radial field compact magnet	Rotor cage bars	Small, medium	Pump, fan, irrigation, transport machines	2,6
2.	Buried magnet rotor	Less chances for demagnetization	Difficult to fabricate	Small, medium	High speed applications	3,21
3.	Bonded ring magnet rotor	Compact magnet, easy to magnetize, reduce cogging torque	Magnets are epoxied or bonded to steel yoke	Medium	Used in low rating motor	4
4.	Circumferential magnet rotor	Line start, Cost effective, low energy density magnets, less cogging	Fluxes are collected and concentrated by soft iron pieces	Medium and large	Pump, molding machines, compressor	5
5.	Inset magnet rotor	High torque/inertia ratio	Expensive to wind	Large rating upto 5MW	Servo system and industrial drive	7,12
6.	Block or arc magnet rotor	Rugged construction, reluctance torque, excellent torque linearity	Consequent pole configuration is used	Medium and large	High performance drives servo drive, spindle tool	8
7.	Spoke magnet rotor	Low cost design, good saliency, best suited to sine fed motor	Higher inertia of the rotor assembly	Medium and high	Spindle tool variable speed drive	9
8.	Halbach magnetized rotor	Ripple free torque, very high speed operation, higher air gap flux density	Special techniques are needed to magnetized the rotor	Small and medium	Used in high speed applications	10
9.	Slotless stator type PM rotor	Zero cogging torque	Costly, difficult to fabricate	Small and medium	Used for high speed turbo application	11
10.	Specially direction magnetized with cage	Line start capability	Braking torque during starting	Medium power rating	Used in compressor and pump drive	13
11.	Inset magnet with damper bar rotor	High torque/inertia ratio	Expensive to wind	Large rating upto 5MW	Industrial drive	14
12.	Radially magnetized rotor	Easy to construct, and less costly	Poor utilization of PM flux	For medium and high	Used in industrial drive	15
13.	Specially direction magnetized rotor	Higher flux density in air gap	Expensive technique	For medium power rating	Medium power rating drives	16
14.	Interior magnet rotor	Reluctance torque, firmly placed magnets	Difficult to fabricate	Small and medium	High speed and higher torque applications.	17, 22
15.	New design of PM Rotor	Higher air gap magnetic field is produced	Intricate construction, requires special production techniques	Medium and large power rating	Wide range of frame size motors efficient integral horse-power drives	18
16.	Hybrid magnetized rotor	Line start capability	Rotor cage bars are needed	Medium and high	Compressors and fans	19
17.	Classical configuration buried PM rotor	Suitable for rapid acceleration and deceleration	Require high energy density magnets	Large rating upto 5MW	High speed drive, servo application	20
18.	Bread loaf magnets type rotor	Lower cost	Special geometry is needed	Small and medium	Low speed drives	23
19.	Tangentially magnetized rotor	Less cogging torque	Difficult to fabricate	Small and medium	High performance servo drives	24
20.	Axial flux PM rotor	Easily magnetized, low cost and zero cogging torque	Iron losses increases with higher speed	Medium	Medium speed, medium power application	25,26
21.	Claw pole machines	Use concentrated winding for high torque	Generally use with single phase system	Low and medium	Timer circuit, car alternators	27
22.	Disc motor	Low cost, smooth rotation with zero cogging	Excessive eddy current losses in the stator above 1000 rpm	Low and medium	Record players, VCR players, CD players and floppy disc drives	28

REFERENCES

1. T Kenjo and S Nagamori. 'Permanent Magnet and Brushless DC Motors'. Clarendon Press, Oxford, 1985.
2. T J E Miller. 'Brushless Permanent Magnet and Reluctance Motor Drives'. Clarendon Press, Oxford, 1989.
3. P Pillay. 'Performance and Design of Permanent Magnet AC Motor Drives'. *Tutorial Course Presented in IEEE Industrial Application Society Conference*, San-Diego, 1989.
4. Y Dote and S Kinoshita. 'Brushless Servomotors Fundamentals and Applications'. Clarendon Press, Oxford, 1990.
5. J R Hendershot and T J E Miller. 'Design of Brushless Permanent -Magnet Motors'. *Magna Physics Publishing and Clarendon Press*, Oxford, 1994.
6. E S Hamdi. 'Design of Small Electrical Machines'. *John Willey and Sons Ltd*, West Sussex, England, 1994.
7. D C Hanselman. 'Brushless Permanent-Magnet Motor Design'. *Morgan-Hill*, New York, 1994.
8. K Rajashekara, A Kawamura and K Matsuse. 'Sensorless Control of AC Motor Drives'. *IEEE Press*, New York, 1996, pp 259-268.
9. B K Bose. 'Power Electronics and Variable Frequency Drives, Technology and Applications'. *IEEE Press*, New York, 1997.
10. P Vas. 'Sensorless Vector and Direct Torque Control'. *Oxford University Press*, New York 1998.
11. I Boldea and S A Nasar. 'Electric Drives'. *CRC Press*, Boca Raton, 1999.
12. J F Gieras and M Wing. 'Permanent Magnet Motor Technology'. *Marcel Dekker Inc*, New York, 2002.
13. M P Kazmierkowski, R Krishnan and F Blaabjerg. 'Control in Power Electronics Selected Problem'. *Academic Press*, San Diego, 2002.
14. V B Honsinger. 'Permanent Magnet Machines: Asynchronous Operation'. *IEEE Transactions on Power Appar System*, vol 99, no 4, July, 1980, pp1503-1509.
15. M A Rahaman. 'Permanent Magnet Synchronous Motors- A Review of State of Design Art'. *Proceedings of ICEM'86*, Athens, 1980, pp 312-319.
16. J Liu and P D Wagner. 'Permanent Magnet Synchronous Motor Rotor'. *US Patent no. 4358696*, vol 9 November, 1982.
17. D Pauly, G Pfaff and A Weschta. 'Brushless Servo Drive with Permanent Magnet Motors or Squirrel Cage Induction Motors- a Comparison'. *Conference Record of IEEE-IAS Annual Meeting*, 1984, pp 503-509.
18. S Ogasawara, Mo Nishimura, H Akagi, A Nabae and Y Nakanishi. 'A High Performance ac Servo System with Permanent Magnet Synchronous Motor'. *Proceedings of IECON'84*, 1984, pp 1111-1116.
19. K J Binns and C P Riley. 'The Scope for Development of Permanent Magnet Machines in the Light of New Materials'. *Proceedings of ICEM'86*, 1986, pp 1061-1062.
20. D F Gosden. 'Some Preliminary Tests on the Comparative Performance of a Permanent Magnet Motor and a Squirrel Cage Induction Motor'. *Electrical Energy Conference 1987*, Adelaide, October, 1987, pp 12-15.
21. D J Gritter, W K O'Neil and D Turner. 'Ferrite Permanent Magnet Electrical Machine and the Application thereof within Vehicle Drives'. *US Patent no 4651066*, March 1987.
22. P Pillay and P Freere. 'Literature Survey of Permanent Magnet ac Motors and Drives'. *Conference Record of IEEE-IAS Annual Meeting*, vol 1, 1989, pp 74-84.
23. T Low, M A Jabbaar and M A Rahaman. 'Permanent Magnet Motors for Brushless Operation'. *IEEE Transactions on Industry Application*, vol 26, no 1, January 1990, pp124-129.
24. G Nerowski, K Plackner, B Piepenbreier and H J Tolle. 'New Permanent Field Synchronous Motor with Integrated Inverters'. *Proceedings of ICEM'90*, 1990, pp 124-131.
25. G B Kliman. 'Composite Rotor Lamination for use in Reluctance Homopolar and Permanent Magnet Motor'. *US Patent no 4916346*, April 1990.
26. B Singh. 'Recent Advances in Permanent Magnet Brushless DC Motors'. *Sadhana*, vol 22, no 6, December 1997, pp 837-853.
27. B J Chalmers, E Spooner, O Honorati, F Crescimbin and F Caricchi. 'Compact Permanent Magnet Machines'. *Electric Machines and Power Systems*, vol 25, 1997, pp 635-648.
28. J S Hsu. 'Flux Guide for Permanent Magnet Machines'. *IEEE Transactions on Energy Conversion*, vol 16, no 2, June 2001, pp 186- 191.
29. E Richter. 'The Proper Magnet Characteristics for Industrial PM Machines'. *Proceedings of Motor Convention*, 1982, pp 564-581.
30. N A Demerdash, R H Miller and T W Nehl. 'Comparison Between Features and Performance Characteristics of Fifteen hp Samarium Cobalt and Ferrite Based Brushless dc Motors Operated by Same Power Conditioner'. *IEEE Transactions on PAS*, vol 102, no 1, January 1983, pp 104 - 112.
31. T W Neumann and R E Tompkins. 'Line Start Motor Designed with Nd-Fe-B Permanent Magnet'. *8th International Workshop on Rare Earth Magnets and their Application*, Dayton, Ohio, 1985, pp 77-89.
32. E Richter, T J E Miller, T W Neumann and T L Hrdson. 'The Ferrite Permanent Magnet ac Motor- A Technical and Economical Assessment'. *IEEE Transactions on Industry Application*, vol 21, no 4, May 1985, pp 644-650.
33. G Henneberger, H Harer and W Schleuter. 'A New Generation of Servomotors with Rare Earth Magnets'. *Proceedings of ICEM*, 1986, pp1083-1086.
34. W Wende, G Jingcun, X Gouliang and C Yong. 'On High Efficiency and Energy-saving dc Brushless Motors'. *Electrical Energy Conference 1987*, Adelaide, October 1987, pp 499-502.
35. I Dudzikoweki and W Stachowiak. 'The Analysis of the Influence of Magnetic Circuit Structure on the Parameters of dc Machines Excited by Ferrite Magnets'. *Proceedings of IEE ICEMD'87*, 1987, pp 265-269.
36. V S Ramsden and H T Nguyen. 'Brushless dc Motors using Neodymium Iron Boron Permanent Magnets'. *Electrical Energy Conference 1987*, Adelaide, October 1987, pp 22-27.
37. T M Hijazi and N A Demerdash. 'Impact of the Addition of a Rotor Mounted Damper Bar Cage on the Performance of Samarium Cobalt Permanent Magnet Brushless dc Motor Systems'. *IEEE Transactions on Energy Conversion*, vol 3, no 4, December 1988, pp 890-898.
38. K J Binns, A A Hameed and F B Chaaban. 'A Canned Solid Rotor Permanent Magnet Machine with Skewed-radial Neodymium-iron-boron Magnets'. *Proceedings of IEE-ICEMD'89*, 1989, pp 56-60.
39. L M C Mhango. 'Benefits of Nd-Fe-B Magnet in Brushless dc Motor Design for Aircraft Applications'. *Proceedings of IEE-ICEMD'89*, pp 76-79.
40. G W Mclean. 'Brushless dc Drives using Claw Type Stator and Disc Rotor'. *Proceedings of IEE*, vol 126, no 7, July 1973, pp 683-689.
41. K J Binns, W R Barnard and M A Jabbar. 'Hybrid Permanent Magnet Synchronous Motors'. *Proceedings of IEE*, vol 125, no 3, March 1978, pp 203-208.
42. P D Evans and J F Eastham. 'Disc Geometry Homopolar Synchronous Machine'. *Proceedings of IEE*, vol 127, no 5, Part-B, September 1980, pp 299-307.

43. K J Binns and M A Jabbar. 'High Field Self Starting Permanent Magnet Synchronous Motors'. *Proceedings of IEE*, vol 128, no 3, Part B, May 1981, pp 157-160.
44. B Sneyers, D W Novotny and T A Lipo. 'Field Weakening in Buried Permanent Magnet ac Motor Drives'. *IEEE Transactions on Industry Application*, vol 21, March 1985, pp 398-407.
45. T J E Miller. 'Single-phase Permanent-magnet Motor Analysis'. *IEEE Transactions on Industry Application*, vol 21, no 4, May 1985, pp 551- 58.
46. A M Osheiba and M A Rahaman. 'Transient Performance of Hysterisis Motors with Ferrite Magnets'. *Electric Machines and Power Systems*, vol 11, 1986, pp 147-157.
47. L Sack. 'The Reluctance Motor in Comparison with Permanent Magnet Synchronous Motor in Brushless Servo Drives'. *Proceedings of ICEM'86*, 1986, pp 1048-1051.
48. H Bausch. 'Large Power Variable Speed ac Machines with Permanent Magnet Excitation'. *Electrical Energy Conference 1987*, Adelaide, October 1987, pp 266-273.
49. H Weh and N Boules. 'Field Analysis for a High Power, High Speed Permanent Magnet Synchronous Machine of the Disc Construction Type'. *Electric Machines and Power Systems*, vol 5, 1979, pp 225-37.
50. R Hanitsch. 'Disc-type Motor with High Energy Permanent Magnets'. *Proceedings of IEE ICEMD'87*, 1987, pp 255-259.
51. R Krishnan. 'Selection Criteria for Servo Motor Drives'. *IEEE Transactions on Industry Application*, vol 23, no 2, March 1987, pp 270-275.
52. R S Colby. 'Classification of Inverter Driven Permanent Magnet Synchronous Motors'. *Record IEEE-IAS Annual Meeting*, 1988, pp 1-6.
53. B K Bose. 'A High Performance Inverter Fed Drive System of an Interior Permanent Magnet Synchronous Machine'. *IEEE Transactions on Industry Application*, vol 24, no 6, November 1988, pp 987-997.
54. M Osheiba, J Qian and M A Rahaman. 'Performance of Hysteresis Permanent Magnet Motors'. *Electric Machines and Power Systems*, vol 16, 1989, pp 265-280.
55. T Alasuvanto and T Jokinen. 'Comparison of Four Different Permanent Magnet Rotor Constructions'. *Proceedings of ICEM'90*, 1990, pp 1034-1039 .
56. B J Chalmers. 'Performance of Interior Type Permanent Magnet Alternator'. *IEE Proceedings of Electric Power Application*, vol 141, no 4, July 1994, pp 186-190.
57. Y Takeda, M Sanada, S Morimoto, T Hirasu and K Taniguchi. 'Cylindrical Linear Pulse Motor with Interior Permanent Magnet Mover'. *IEEE Transactions on Industry Application*, vol 30, no 1, January 1994, pp 141-145.
58. K Hameyer and R J M Belmans. 'Permanent Magnet Excited Brushed dc Motors'. *IEEE Transactions on Industry Electronics*, vol 43, no 2, April 1996, pp 247-55.
59. M A Jabbar. 'Disk Drive Spindle Motors and their Controls'. *IEEE Transactions on Industry Electronics*, vol 43, no 2, April 1996, pp 276-284.
60. B S P Perera and M F Islam. 'Interior Permanent Magnet Motor Having Several Improved Features'. *Electric Machines and Power Systems*, vol 25, 1997, pp 1135-1144.
61. D Grenier, L A Dessaint, O Akhrif, Y Bonnassieux and B L Pioufle. 'Experimental Non-linear Torque Control of a Permanent Magnet Synchronous Motor using Saliency'. *IEEE Transactions on Industry Electrnics*, vol 44, no 5, October 1997, pp 680-687.
62. K J Binns and A Kurdali. 'Permanent Magnet ac Generators'. *Proceedings of IEE*, vol 126, no 7, July 1973, pp 690-696.
63. S Noodleman. 'New Rotor Concept for a 60 kVA Permanent Magnet Alternator'. *Proceedings of Motor Convention'82*, 1982, pp 552-563.
64. G A J Amaratunga, P P Acarnley and P G McLaren. 'Optimum Magnetic Circuit Configurations for Permanent Magnet Aerospace Generators'. *IEEE Transactions on Aerospace Electronics System*, vol 21, no 2, March,1985, pp 2803-2805.
65. G Henneberger. 'Application Opportunities for Permanent Magnets in Starter Motors and Alternators for Passenger Cars'. *Proceedings of IEE ICEM'86*, 1986, pp 1079-1082.
66. G Amaratunga and P McLaren. 'Permanent Magnet Generators for Aerospace Applications: Optimization of Power to Weight Ratio'. *Proceedings of IEE-ICEM'87*, pp 335-339.
67. B J Spooner, M M Chalmers, El-missiry and I Kitzmann. 'The Design of an Axial-flux Slotless Toroidal-stator Permanent-magnet Machine for Starter/Alternator Applications'. *Proceedings of 25th Universities Power Engineering Conference*, Aberdeen, September 1990, pp 171-174.
68. E Spoonetr and B J Chalmers. 'TORUS: A Slotless Toroidal Stator Permanent Magnet Generator'. *Proceedings of IEE*, vol 139, no 6, Part-B, November 1992, pp 497-506.
69. F Caricchi, F Crescimbin, O Honorati, G L Bianco and E Santini. 'Performance of Coreless Winding Axial Flux Permanent Magnet Generator with Power Output at 400 Hz, 3000 r/min'. *IEEE Transactions on Industry Application*, vol 34, no 6, November 1998, pp 1263-1269.
70. N Boules and H Weh. 'Machine Constants and Design Considerations of a High Power High Speed Permanent Magnet Disc Type Synchronous Machine'. *Electric Machines and Power Systems*, vol 5, 1980, pp 113-123.
71. A Levran and E Levi. 'Design of Polyphase Motors with PM Excitation'. *IEEE Transactions on Magnetics*, vol 201, no 3, May 1984, pp 507-515.
72. M A Rahaman. 'Design and Analysis of Large Permanent Magnet Synchronous Motors'. *8th Interernational Workshop on Rare Earth Magnets and their Application*, Dayton, Ohio, 1985, pp 67-75.
73. N Boules. 'Field Analysis of PM Synchronous Machines with Buried Magnet Rotor'. *Proceedings on ICEM'86*, 1986, pp 1063-1066.
74. M A Jabbar. 'Mains Voltage Permanent Magnet Motors for Appliances: Aspects of Design and Development'. *Electrical Energy Conference 1987*, Adelaide, October 1987, pp 272-277.
75. M A Jabbaar. 'Design and Operational Aspects of High Speed Appliance Motor using Ceramic Magnets'. *Proceedings of IEE ICEMD'87*, 1987, pp 311-315.
76. A M Sitzia and B J Chalmers. 'Electromagnetic Design of Brushless dc Motor with Slotless Stator'. *Proceedings of IEE ICEMD'87*, 1987, pp 260-264.
77. G R Slemon. 'On the Design of High Performance Surface Mounted PM Motors'. *IEEE Transactions on Industry Application*, vol 30, no 1, January 1994, pp 134-140.
78. M Ooshima, A Chiba, T Fukao and M A Rahman. 'Design and Analysis of Permanent Magnet Type Bearingless Motors'. *IEEE Transactions on Industry Electronics*, vol 3, no 2, April 1996, pp 292-98.
79. S Jang, S Jeong, D Ryu and S Choi. 'Design and Analysis of High Speed Slotless PM Machine with Halbach Array'. *IEEE Transactions on Magnetics*, vol 37, no 4, July 2001, pp 2827-2830.
80. J Cros and P viarouge. 'Synthesis of High Performance PM Motors with Concentrated Windings'. *IEEE Transactions on Energy Conversion*, vol 17, no 2, June 2002, pp 248- 253.
81. G Brentani. 'The Effects of the Torque Ripple and Cogging Torque on the Instantaneous Speed Variation of a Brushless dc Motor'. *Proceedings of Motor Conference '85*, 1985, pp 20-30.

82. T R England. 'Unique Surface Wound Brushless Servo with Improved Torque Ripple Characteristics'. *IEEE Transactions on Industry Application*, vol 24, no 6, November 1988, pp 987-997.
83. T Li and G Slemon. 'Reduction of Cogging Torque in Permanent Magnet Motors'. *IEEE Transactions on Magnetics*, vol 24, no 6, November 1988, pp 2901-2903.
84. T Ishikawa and G R Slemon. 'A Method of Reducing Ripple Torque in Permanent Magnet Motors without Skewing Interlacing'. *IEEE Transactions on Magnetics*, vol 29, no 2, March 1993, pp 2028-2031.
85. T M Jahns and W L Soong. 'Pulsating Torque Minimization Techniques for Permanent Magnet ac Motor Drives- A Review'. *IEEE Transactions Industry Electronics*, vol 43, no 2, April 1996, pp 321-330.
86. K T Kim, K S Kim, S Hwang, T Kim and Y Jung. 'Comparison of Magnetic Forces for IPM and SPM Motor with Rotor Eccentricity'. *IEEE Transactions on Magnetics*, vol 37, no 5, September 2001, pp 3448 -3451.
87. S Hwang, J Eom, Y Jung, Dec and B Kang. 'Various Design Techniques to Reduce Cogging Torque by Controlling Energy Variation in Permanent Magnet Motors'. *Transactions on Magnetics*, vol 37, no 4, July 2001, pp 2806-2809.
88. P Campbell. 'Principal of a Permanent Magnet Axial Field dc Machine'. *Proceedings of IEE*, vol 121, no 12, pp 1489-1494, December 1974.
89. D Platt. 'Permanent Magnet Synchronous Motor with Axial Flux Geometry'. *IEEE Transactions on Magnetics*, vol 25, no 4, July 1989, pp 3076-3079.
90. S Geetha and D Platt. 'Axial Flux Permanent Magnet Servo Motor with Sixteen Poles'. *Records of IEEE-LAS Annual Meeting*, 1992, pp 286-291
91. R Hanitsch and D S Choi. 'Axial Flux Permanent Magnet Motor with Etched Windings and Magnetoresistive Rotor Position Sensing'. *Proceedings of IEE ICEMD'93*, 1993, pp 448-451.
92. M M Elmissiry and S Chari. 'Performance of Toroidal Stator, Axial Flux Brushless dc Motor under Dynamic Conditions of Operation'. *Proceedings of IEE ICEMD'93*, 1993, pp 612-618.
93. F Caricchi, F Crescimbin and E Santini. 'Basic Principle and Design Criteria of Axial-flux PM Machines Having Counter-rotating Rotors'. *Conference Records of IEEE-LAS Annual Meeting*, 1994, pp 247-253.
94. F Caricchi, F Crescimbin, E Fedeli and G Noioa. 'Design and Construction of a Wheel-directly-coupled Axial-flux PM Motor Prototype for Evs'. *Conference Records of IEEE-LAS Annual Meeting*, 1994, pp 254-261.
95. F Caricchi, F Crescimbin, F Mezzetti and E Santini. 'Multistage Axial Flux PM Machine for Direct Wheel Drive'. *IEEE Transactions on Industry Application*, vol 32, no 4, July 1996, pp 882-888.
96. L Soderlund, A Koski, H Vihriala, J T Eriksson and R Perala. 'Design of an Axial Flux Permanent Magnet Wind Power Generator'. *Proceedings of IEE ICEMD'97*, 1997, pp 224 -228
97. F Caricchi, F Crescimbin, E Santini and C Santucci. 'Influence of the Radial Variation of the Magnet Pitch in Slotless Permanent Magnet Axial Flux Motors'. *Records of IEEE-LAS Annual Meeting*, 1997, pp 18-23.
98. F Caricchi, F Crescimbin, O Honorzti, G Lo Bianco and E Santini. 'Performance of Coreless-winding Axial-flux Permanent-magnet Generator with Power Output at 400 Hz-3000 rev/min'. *IEEE Transactions on Industry Application*, vol 34, no 6, November 1998, pp 1263-1269.
99. B J Chalmers and E Spooner. 'An Axial-flux Permanent-magnet Generator for a Gearless Wind Energy System'. *IEEE Transactions on Energy Conversion*, vol 14, no 2, June 1999, pp 251-257.
100. L Jian, O Dinyu, T A Lipo, L Shuxiang and S Huang. 'Axial Flux Circumferential Current Permanent Magnet (AFCC) Machine'. *Records of IEEE-LAS Annual Meeting*, 1998, pp 144 -151.
101. M Aydin, H Surong Huang and T A Lipo. 'Torque Quality and Comparison of Internal and External Rotor Axial Flux Surface-magnet Disc Machines'. *Proceedings of IEEE IECON'01*, 2001, pp 1428-1434.
102. R J Hill-Cottingham, PC Coles, J F Eastham, F Profumo, A Tenconi, G Gianolio and M Cerchio. 'Plastic Structure Multi-disc Axial Flux PM Motor'. *Records of IEEE-LAS Annual Meeting*, 2002, pp 1274 -1280.
103. A Cavagnino, M Lazzari, F Profumo and A Tenconi. 'A Comparison Between the Axial Flux and the Radial Flux Structures for PM Synchronous Motors'. *IEEE Transactions on Industry Application*, vol 38, no 6, December 2002, pp 1517-1524.
104. O Ronghai, M Aydin and T A Lipo. 'Performance Comparison of Dual-rotor Radial-flux and Axial-flux Permanent-magnet BLDC Machines'. *Proceedings of IEEE IEMDC'03*, 2003, pp 1948-1954.
105. P Campbell, M Chari and J D'Angelo. 'Three-dimensional Finite Element Solution of Permanent Magnet Machines'. *IEEE Transactions on Magnetics*, vol 17, no 6, pp 2997 -2999, Nov 1981.
106. N Demerdash, F Fouad and T Nehl. 'Determination of Winding Inductances in Ferrite Type Permanent Magnet Electric Machinery by Finite Elements'. *IEEE Transactions on Magnetics*, vol 18, no 6, November 1982, pp 1052-1054.
107. N A O Demerdash and M A Alhamadi. 'Three Dimensional Finite Element Analysis of Permanent Magnet Brushless dc Motor Drives-status of the State of the Art'. *IEEE Transactions on Industry Electronics*, vol 43, no 2, April 1996, pp 268-275.
108. J F Eastham, D M Ionel, M J Balchin, T Betzer and E Demeter. 'Finite Element Analysis of an Interior-magnet Brushless dc Machine with a Step-Skewed Rotor'. *IEEE Transactions on Magnetics*, vol 33, no 2, March 1997, pp 2117-2119.
109. W Yong, K T Chau, C C Chan and J Z Jiang. 'Transient Analysis of a New Outer-rotor Permanent-magnet Brushless dc Drive using Circuit-field-torque Coupled Time-stepping Finite-element Method'. *IEEE Transactions on Magnetics*, vol 38, no 2, March 2002, pp 1297-1300.
110. K Gyu-Hong Kang, H Jin, N Hyuk, H Jung-Pyo and K Gyu-Tak. 'Analysis of Irreversible Magnet Demagnetization in Line-start Motors Based on the Finite-element Method'. *IEEE Transactions on Magnetics*, vol 39, no 3, May 2003, pp 1488 -1491.
111. M Aydin, S Huang and T A Lipo. 'Performance Evaluation of an Axial Flux Consequent Pole PM Motor using Finite Element Analysis'. *Proceedings of IEMDC'03*, 2003, pp 1682-1687.
112. T Ishikawa, M Matsuda and M Matsunami. 'Finite Element Analysis of Permanent Magnet Type Stepping Motors'. *IEEE Transactions on Magnetics*, vol 34, no 5, September 1998, pp 3503 -3506.
113. C Hong-Soon and B Soo-Hyun. 'Finite Element Analysis of an Anisotropic Ferrite Bonded Magnet for BLDC Motor Design'. *Proceedings of ICEM'01*, 2001, pp 1170 -1173.
114. M G B Venturini. 'Integrated High Power Density Brushless Servo Drives for Avionic Fly by Wire and Satellite Applications'. *Proceedings of Motor-Conference'82*, 1982, pp 163-171.
115. C C Chan. 'Axial Field Electrical Machines-design and Applications'. *IEEE Transactions on Energy Conversion*, vol 2, no 2, June 1987, pp 294 -300.
116. R M Crowder. 'The Application and Control of Brushless dc Motors in High Power Robotic Joints'. *Proceedings of IEE PEVSD'88*, 1988, pp 253-257.
117. V S Ramsden. 'Permanent Magnet Motor Developments and Markets'. *Journal of Electrical and Electronics Engineering Australia*, vol 9, no 3, September 1989, pp 118-123.
118. D Patterson and R Spee. 'The Design and Development of an Axial Flux Permanent Magnet Brushless dc Motor for Wheel Drive in a Solar Powered Vehicle'. *Records of IEEE-LAS Annual Meeting*, 1994, pp 188 -195.

119. D Patterson and R Spee. 'The Design and Development of an Axial Flux Permanent Magnet Brushless dc Motor for Wheel Drive in a Solar Powered Vehicle'. *IEEE Transactions on Industry Application*, vol 31, no 5, September 1995, pp 1054-1060.
120. F Caricchi, F Crescimbinì and A Di Napoli. 'Prototype of Innovative Wheel Direct Drive with Water-cooled Axial-flux PM Motor for Electric Vehicle Applications'. *Proceedings of IEEE APEC '96*, 1996, pp 764-770.
121. F Profamo, Z Zhang and A Tenconi. 'Axial Flux Machines Drives: A New Viable Solution for Electric Cars'. *IEEE Transactions on Industry Electronics*, vol 44, no 1, February 1997, pp 39-45.
122. E Muljadi, C P Butterfield and W Yih-Huie. 'Axial-flux Modular Permanent-magnet Generator with a Toroidal Winding for Wind-turbine Applications'. *IEEE Transactions on Industry Application*, vol 35, no 4, July 1999, pp 831 -836.
123. F Caricchi, F Crescimbinì and O Honorati. 'Modular, Axial-flux, Permanent-magnet Motor for Ship Propulsion Drives'. *IEEE Transactions on Energy Conversion*, vol 14, no 3, September 1999, pp 673-679.
124. R J Hill-Cottingham, P C Coles, J F Eastham, F Profumo, A Tenconi and G Gianolio. 'Novel Axial Flux Machine for Aircraft Propeller Drive: Design and Modelling'. *IEEE Transactions on Magnetics*, vol 38, no 5, September 2002, pp 3003-3005.
125. B C Mecrow, A G Jack, D J Atkinson, P G Dickinson and S Swaddle. 'High Torque Machines for Power Hand Tool Applications'. *Proceedings of IEE PEMD'02*, pp 644-649, 2002.
126. L Cheng-Tsung, T S Chiang, J F Diaz Zamora and S C Lin. 'Field-oriented Control Evaluations of a Single-sided Permanent Magnet Axial-flux Motor for an Electric Vehicle'. *IEEE Transactions on Magnetics*, vol 39, no 5, September 2003, pp 3280-3282.